

2.1 # 16, 36, 46, 52, 72, 74

15, 19, 33, 35, 45, 53, 71,

15) $f(x) = 6 - 2x$, (2, 2)

$y = mx + b$

$$\begin{aligned}f'(x) &= \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{[6 - 2(x + \Delta x)] - [6 - 2x]}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{6 - 2x - 2\Delta x - 6 + 2x}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{-2\Delta x}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} -2, \quad \Delta x \neq 0 \\&= -2\end{aligned}$$

19) $f(x) = x^2 - 1$, (2, 3) *

$$\begin{aligned}f'(x) &= \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{[(x + \Delta x)^2 - 1] - (x^2 - 1)}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x + (\Delta x)^2 - x^2 - 1}{\Delta x} \\&= \lim_{\Delta x \rightarrow 0} \frac{2x\Delta x + (\Delta x)^2}{\Delta x}\end{aligned}$$

At $x = 2$

$$\begin{aligned}&= \lim_{\Delta x \rightarrow 0} (2x) \\&= 2(2)\end{aligned}$$

$$= 2x = 4$$

$$33. h(t) = \sqrt{t-1}$$

$$h'(t) = \lim_{\Delta t \rightarrow 0} \frac{h(t+\Delta t) - h(t)}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} \frac{\sqrt{(t+\Delta t)-1} - \sqrt{t-1}}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} \left[\frac{(t+\Delta t-1) - (t-1)}{\Delta t(\sqrt{t+\Delta t-1} + \sqrt{t-1})} \right]$$

$$= \lim_{\Delta t \rightarrow 0} \left[\frac{\Delta t}{\Delta t(\sqrt{t+\Delta t-1} + \sqrt{t-1})} \right]$$

$$= \lim_{\Delta t \rightarrow 0} \left[\frac{1}{\sqrt{t+\Delta t-1} + \sqrt{t-1}} \right]$$

$$= \frac{1}{\sqrt{t-1} + \sqrt{t-1}}$$

$$= \frac{1}{2\sqrt{t-1}}$$

$$35. f(t) = t^3 - 12t$$

$$f'(t) = \lim_{\Delta t \rightarrow 0} \frac{f(t+\Delta t) - f(t)}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} \frac{[(t+\Delta t)^3 - 12(t+\Delta t)] - (t^3 - 12t)}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} \frac{(t^3 + 3t^2\Delta t + 3t(\Delta t)^2 + (\Delta t)^3 - 12t - 12\Delta t) - (t^3 - 12t)}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} \frac{3t^2\Delta t + 3t(\Delta t)^2 + (\Delta t)^3 - 12\Delta t}{\Delta t}$$

$$= \lim_{\Delta t \rightarrow 0} [3t^2 + 3t\Delta t + \frac{(\Delta t)^2 - 12}{\Delta t}]$$

$$= 3t^2 - 12$$

$$45) f(x) = \frac{1}{x}, \quad (1, 1)$$

$$f(x) = x^{-1}$$

$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^{-1} - x^{-1}}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{\frac{1}{x + \Delta x} - \frac{1}{x}}{\Delta x} = \lim_{\Delta x \rightarrow 0} \frac{\frac{x}{x(x + \Delta x)} - \frac{x + \Delta x}{x(x + \Delta x)}}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{x - (x + \Delta x)}{x(x + \Delta x) \Delta x} = \lim_{\Delta x \rightarrow 0} \frac{-\Delta x}{x \cancel{\Delta x}(x + \Delta x)}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{-1}{x(x + \Delta x)} = \frac{-1}{x^2}$$

$$f'(1) = \frac{-1}{(1)^2} = -1$$

$$y - y_0 = m(x - x_0) \quad (1, 1)$$

$$y - 1 = -1(x - 1)$$

$$y - 1 = -1x + 1$$

$$y = -x + 2$$

71) The slope of $f(x) = x^2$ is different at every point.

$$\begin{aligned}\lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^2 - x^2}{\Delta x} &= \lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x + (\Delta x)^2 - x^2}{\Delta x} \\ &= \lim_{\Delta x \rightarrow 0} (2x + \Delta x) \\ &= 2x\end{aligned}$$

x can be any real number

$$f'(x) = 2x$$

So the slope is different
at every point.

