

$$P(A_4 | R_3) = \frac{P(A_4 \text{ and } R_3)}{P(R_3)} = \frac{\frac{36}{1164}}{\frac{320}{1164}} = \frac{0.031}{0.275} = 0.1125$$

$$P(R_3) = \frac{320}{1164}$$

$$P(A_2) = \frac{402}{1164}$$

$$P(A_2 \text{ and } R_2) = \frac{170}{1164}$$

		Rank				
		Full professor R_1	Associate professor R_2	Assistant professor R_3	Instructor R_4	Total
Age (yr)	Under 30 A_1	A1 and R1 2	3	57	A1 and R4 6	68
	30-39 A_2	52	170	163	17	402
	40-49 A_3	156	125	61	6	348
	50-59 A_4	145	68	A4 and R3 36	4	253
	60 & over A_5	75	15	3	0	93
	Total	430	381	320	33	1164

$$\frac{36}{320}$$

Cells

R_3 = the event that an faculty's rank is Assistant Prof.

A_2 = the event that the faculty's age is 30-39.

A_2 and R_2

	C1	C2	Total
R1	3	x=7	10
R2	z=8	7	y=15
Total	a=11	b=14	25

$$3 + x = 10$$

$$x = 7$$

$$10 + y = 25$$

$$y = 15$$

Joint probabilities (based on cells)

$$z + 7 = 15$$

$$P(R_2) = \frac{15}{25} = \frac{3}{5} = 0.6 \quad z = 8$$

$$P(C_1) = \frac{11}{25}$$

$$P(R_1 \text{ and } C_1) = \frac{3}{25}$$